# A 2V CMOS Capacitorless Current-Tunable All-Pass Filter using Current Mirrors

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#### Abstract

A 2V CMOS capacitorless current-tunable all-pass filter using current mirrors is presented through the use of the MOS internal capacitances. The frequency  $f_o$  where the magnitude and phase shift of the transfer function are approximately 0 dB and -90°, respectively, is tunable through the bias current. The maximum useful  $f_o$  is in excess of 700MHz depending on the internal parameters.

## 1. Introduction

All-pass filters are utilised in many applications such as in sinusoidal quadrature oscillators. Most techniques of integrable allpass filters employ relatively large external therefore capacitors and the operating frequencies are not relatively high [1-4]. Recently, capacitorless techniques have exploited not only the paracitic capacitances of BJTs for high-frequency all-pass filters [5] or integrators [6], but also the internal capacitances of MOS for high-frequency bandpass filters [7] or switched-current circuits [8].

In this paper, a 2V high-frequency CMOS capacitorless current-tunable all-pass filter using current mirrors is presented through the use of the MOS internal capacitances. The frequency  $f_o$  where the magnitude and phase shift of the transfer function are approximately 0 dB and  $-90^\circ$ , respectively, is tunable through the bias current. The maximum useful  $f_o$  is in excess of 700 MHz depending on the internal parameters.

#### 2. Circuit Descriptions

Figure 1 shows the circuit of the CMOS capacitorless current-tunable all-pass filter. The circuit consists of current mirrors formed by five NMOS transistors Q1 to Q5 and three current sources I, 2I and 4I. Q1 to Q3 are identical and the aspect ratios are W/L. The aspect ratios of Q4 and Q5 are separated into two cases. In the first case, the ratios are 16W/L and 32W/L respectively. In the second case, the ratios are 2W/L and 4W/L, respectively. The small signal

input current  $i_{in}$  is applied to the drain of Q1 and the resulting small signal output current  $i_o$  is taken from the drain of Q5.

### 3. Ideal Analysis

For a MOS transistor, the unity current gain frequency  $\omega_T$  is equal to  $g_m/C$  where  $C = (C_{gs} + C_{gd} + C_{gb})$  [9] and  $g_m = (2I)/(V_{GS} - V_T)$ .  $C_{gs}$ ,  $C_{gd}$  and  $C_{gb}$  are the MOS internal capacitances. The subscripts g, s, d and b stand for gate, source, drain and body of a MOS transistor.  $V_{GS}$  is the gate source voltage.  $V_T$  is the usual threshold voltage and I is the bias current. Referring to Figure 1, the small signal current i<sub>x</sub> yields

$$i_{x} = \frac{i_{in}}{1+s\tau_{x}}$$
(1)

where the time constant  $\tau_a = C_a/g_{m1}$ ,  $C_a = (C_{gs} + C_{gb})_1 + (C_{gs} + C_{gd} + C_{gb})_2 + (C_{gs} + C_{gd} + C_{gb})_3$ and  $g_{m1} = (2I) / (V_{GS1} - V_T)$ . The subscripts 1 to 3 refer to Q1 to Q3. Similarly, the small signal current  $i_v$  is equal to

$$i_{y} = \frac{2i_{x}}{1+s\tau_{b}}$$
(2)

where the time constant  $\tau_b = C_b/g_{m4}$ ,  $C_b = (C_{gs} + C_{gb})_4 + (C_{gs} + C_{gd} + C_{gb})_5$  and  $g_{m4} = (21) / (V_{GS4} - V_T)$ . The subscripts 4 and 5 refer to Q4 and Q5. In addition,  $i_y = i_0 + i_x$ . Therefore, the transfer function  $T(s) = i_0/i_{in}$  yields

$$\mathbf{T(s)} = \frac{(1 - s\tau_b)}{(1 + s\tau_a)(1 + s\tau_b)}$$
(3)

For sinusoidal input, the magnitude M and phase shift  $\phi$  of equation (3) are of the form

$$M = -20\log\sqrt{1+\omega^2\tau_a^2} \tag{4}$$

$$\phi = \tan^{-1}(-\omega\tau_b) - \tan^{-1}(\omega\tau_b) - \tan^{-1}(\omega\tau_a)$$
 (5)

Equation (3) can be considered in two cases. In the first case for  $\tau_a \ll \tau_b$ , equation (3) is reduced to a first-order all-pass filter of the form

$$\mathbf{T(s)} \cong \frac{(1-s\tau_b)}{(1+s\tau_b)} \tag{6}$$

In this case, the magnitude and phase shift of equation (6) are 0 dB and  $-90^{\circ}$ , respectively, at the frequency  $\omega = \omega_1$  for

$$\omega_1 = 1/\tau_b = g_{m4}/C_b = (2I) / [(V_{GS4} - V_T)C_b]$$
 (7)

In the second case for  $\tau_a < \tau_b$ , equation (3) may be approximated as an all-pass filter where M described in (4) approaches 0 dB at  $\phi = -90^{\circ}$ and at  $\omega = \omega_o = h\omega_1$  for

$$h = \sqrt{\frac{\tau_b}{2\tau_a + \tau_b}} \tag{8}$$

It can be seen from (7) and (8) that  $\omega_0$  and  $\omega_1$  are tunable through the bias current I and hence the name "current-tunable".

## 4. Simulation Results

The performance of the circuit shown in Figure 1 has been simulated using SPICE and all transistors are in saturation mode. The CMOS transistors are modeled by Alcatel Mietec 0.5  $\mu$ m CMOS C05MD Technology from EUROPRACTICE. The width W and length L are equal to 0.5  $\mu$ m. The supply voltage V<sub>CC</sub> = 2 V and V<sub>T</sub> = 0.68 V. Table 1 shows the internal capacitances of Q1 to Q5. Table 2 shows values of  $\tau_a$  and  $\tau_b$  at I = 20  $\mu$ A.

Table 1.Internal capacitances of Q1 to Q5

	Ratios	$C_{gs}(F.)$	$C_{gd}(F_{\cdot})$	$C_{gb}(F_{.})$
Q1,	W/L	1×10 <sup>-15</sup>	1×10 <sup>-16</sup>	3×10 <sup>-16</sup>
Q2, Q3				
Q4	2W/L	2×10 <sup>-15</sup>	2×10 <sup>-16</sup>	6×10 <sup>-16</sup>
Q5	4W/L	4×10 <sup>-15</sup>	4×10 <sup>-16</sup>	12×10 <sup>-16</sup>
Q4	16W/L	16×10 <sup>-15</sup>	16×10 <sup>-16</sup>	$48 \times 10^{-16}$
Q5	32W/L	32×10 <sup>-15</sup>	32×10 <sup>-16</sup>	96×10 <sup>-16</sup>

Table 2. Values of  $\tau_a$  and  $\tau_b$  at I = 20  $\mu$ A.

	Ratios	current (µA)	V <sub>GS</sub> (V)	$\tau_a$ (10 <sup>-11</sup> s)	$\tau_{b}$ (10 <sup>-11</sup> s)
Q1, Q2, Q3	W/L	I = 20	1.14	4.715	-
Q4	2W/L	I = 20	1.01	-	6.663
Q5	4W/L	2I = 40	1.01	-	
Q4	16W/L	I = 20	0.79	-	18.830
Q5	32W/L	2I = 40	0.79	-	

Let the aspect ratios of Q4 and Q5 be 16W/L and 32W/L, respectively, and represent an approximated example of the all-pass filters described in the first case where  $\tau_a << \tau_b$ . In this case, h = 0.81 where M and  $\phi$  are -0.1 dB and -90°, respectively. For such a case, Figure 2 depicts  $f_o = \omega_o/(2\pi)$  and M at  $\phi = -90^\circ$  versus I using dotted and solid lines for the expected and simulated results, respectively.

On the other hand, let the aspect ratio of Q4 and Q5 be 2W/L and 4W/L, respectively, and represent an example of the approximated all-pass filter described in the second case

where  $\tau_a < \tau_b$ . In this case, h = 0.64 where M and  $\phi$  are -0.7 dB and -90°, respectively. For such a case, Figure 3 shows  $f_o = \omega_o/(2\pi)$  and M at  $\phi = -90^\circ$  versus I using dotted and solid lines for the expected and simulated results, respectively. It can be seen from Figures 2 and 3 that the expected and simulated results are in resonably good fits.

Figure 4 shows the magnitude (dB) and phase shift (degrees) of (6) and (3) versus frequency (Hz) at bias current I = 20  $\mu$ A and 50  $\mu A$  for the first case ( $\tau_a \ll \tau_b$ ) and the second case  $(\tau_a < \tau_b)$ , respectively. It can be seen from Figure 4 that, the frequency  $(f_0)$  at phase shift of  $-90^{\circ}$  for the first case and the second case are approximately 700 MHz and GHz. 2 corresponding respectively. whilst the magnitude are approximately -0.1 dB and -0.7 dB, respectively.

# 5. Discussions

It can be seen from Figures 2 and 3 that  $f_o$ of the first case ( $\tau_a << \tau_b$ ) is lower than  $f_o$  of the second case ( $\tau_a << \tau_b$ ), and the maximum useful  $f_o$ are approximately 700 MHz and 2 GHz, respectively. On the other hand, M of the first case is better than M of the second case but may be further amplified by a wide band amplifier for further use. For applications at high frequencies, the second case ( $\tau_a < \tau_b$ ) can be considered more attractive than the first case ( $\tau_a << \tau_b$ ) in terms of higher value of  $f_o$  if  $\tau_a$  of the two cases are the same.

Under small-signal operation and ideal input and the output current sources, impedances of the circuit shown in Figure 1 are  $Z_{in} =$  $(1/g_{m1}) / (1+s\tau_a)$  and  $Z_{out} \cong r_o/2$ , respectively, where r<sub>o</sub> is a finite resistance of MOS between drain and source occurring from the effect of channel-length modulation. The input impedance is a typical value of approximately 1/gm1 at low frequency. The output impedance can be improved through the use of conventional cascode techniques with an expense of lower fo due to additional internal capacitances.

The ideal current sources shown in Figure 1 can be realized through practical PMOS current sources but the  $f_o$  and magnitude (dB) at -90 degrees versus I may slightly be decreased because of additional capacitance  $C_{ds}$  from a PMOS transistor. However, the source is

connected to the body and therefore  $C_{ds} \cong C_{db}$ where  $C_{db}$  can usually be neglected [10].

## 6. Conclusions

A 2V CMOS capacitorless current-tunable all-pass filter using current mirrors has been presented through the use of the MOS internal capacitances. The frequency  $f_o$  where the magnitude and phase shift of the transfer function are approximately 0 dB and  $-90^\circ$ , respectively, is tunable through the bias current. The maximum useful  $f_o$  is in excess of 700 MHz depending on the internal parameters.

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# 8. References

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Figure 1 : Schematic diagram of the CMOS capacitorless current-tunable all-pass filter.



Figure 2 : Frequency  $f_0$  (Hz) and magnitude M (dB) at  $\phi = -90^\circ$  versus I where the aspect ratios of Q4 and Q5 are, for the first case ( $\tau_a \ll \tau_b$ ), 16W/L and 32W/L, respectively.



Figure 3 : Frequency  $f_0$  (Hz) and magnitude M (dB) at  $\phi = -90^\circ$  versus I where the aspect ratios of Q4 and Q5 are, for the second case ( $\tau_a < \tau_b$ ), 2W/L and 4W/L, respectively.



Figure 4 : Magnitude (dB) and phase shift (degrees) of (6) and (3) versus frequency (Hz) at I = 20 uA and 50 uA for the first case ( $\tau_a \ll \tau_b$ ) and the second case ( $\tau_a \ll \tau_b$ ), respectively.